AN CLASS OF INVISIBLE SPACES

K. P. HART

ABSTRACT. A space, X, is said to have a small diagonal if there is no ω_1 sequence in $X^2 \setminus \Delta(X)$ that converges to $\Delta(X)$. Clearly metrizable spaces (even those with a G_{δ} -diagonal) have small diagonals. An old conjecture states that the converse is true for compact Hausdorff spaces: every csD space (short for compact small Diagonal) is metrizable. Thus far all partial results point in the direction of a positive solution; this means that we have no illustrative/ instructive examples of csD spaces: non-metrizable csD spaces have thus far remained invisible. I will survey older and more recent work on this conjecture.

This represents joint work with Alan Dow.